

# Performance analysis and performance modeling of web-applications

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# Agenda

Motivation for modeling

Performance measurement

Performance modeling

Summary

# Motivation for modeling

Highly integrated systems, many customers

- Enhancing customer satisfaction (by)

- Improving response time

Analysis needs rebuilding infrastructure

- You won't want to analyze in productive environment

- Very expensive

Decision making is often estimated

- gut feeling plus a buffer

- Matches reality?

# Performance measurement

Analyzing a realistic scenario:

After “Freshman student” event

1.600 Students planned their study plan

concurrent and on a 1:1:1-infrastructure  
(1 Web-, 1 App-, 1 DB-Server)

Problems arised:

Slower response times

Even timeouts

No login possible

Not all customers were satisfied!

# Performance measurement

Solution: More hardware

Three Questions:

What is the applicable amount?

Where is the bottleneck?

What can be done in realistic time?

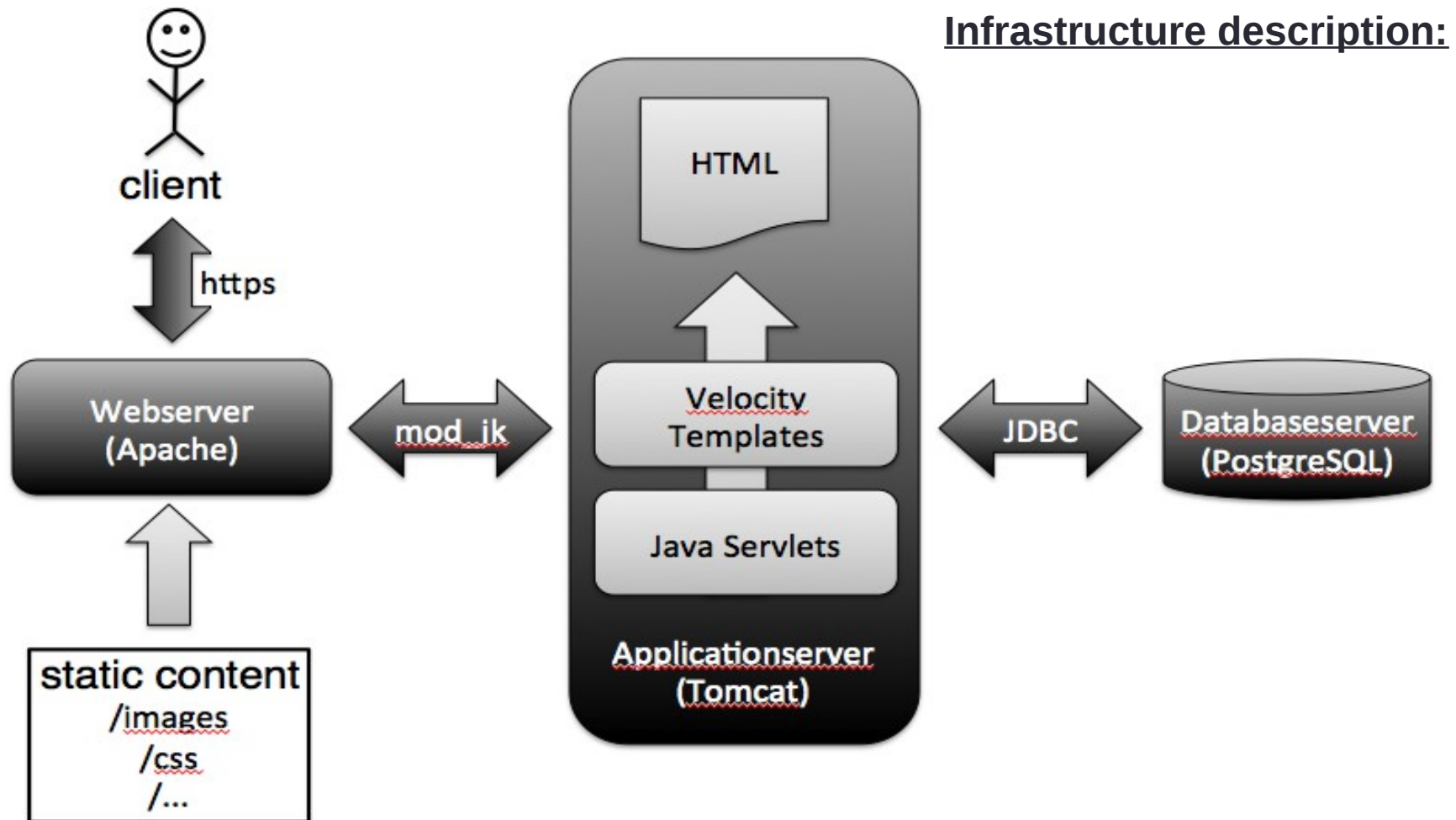
What we have done:

Rebuilding Infrastructure

Simulation of a specific scenario with funkload

Evaluating results

# Performance measurement



# Performance measurement

Simulation scenario:

- Call the start page

- Login with a random user

- Navigate through the lecture index

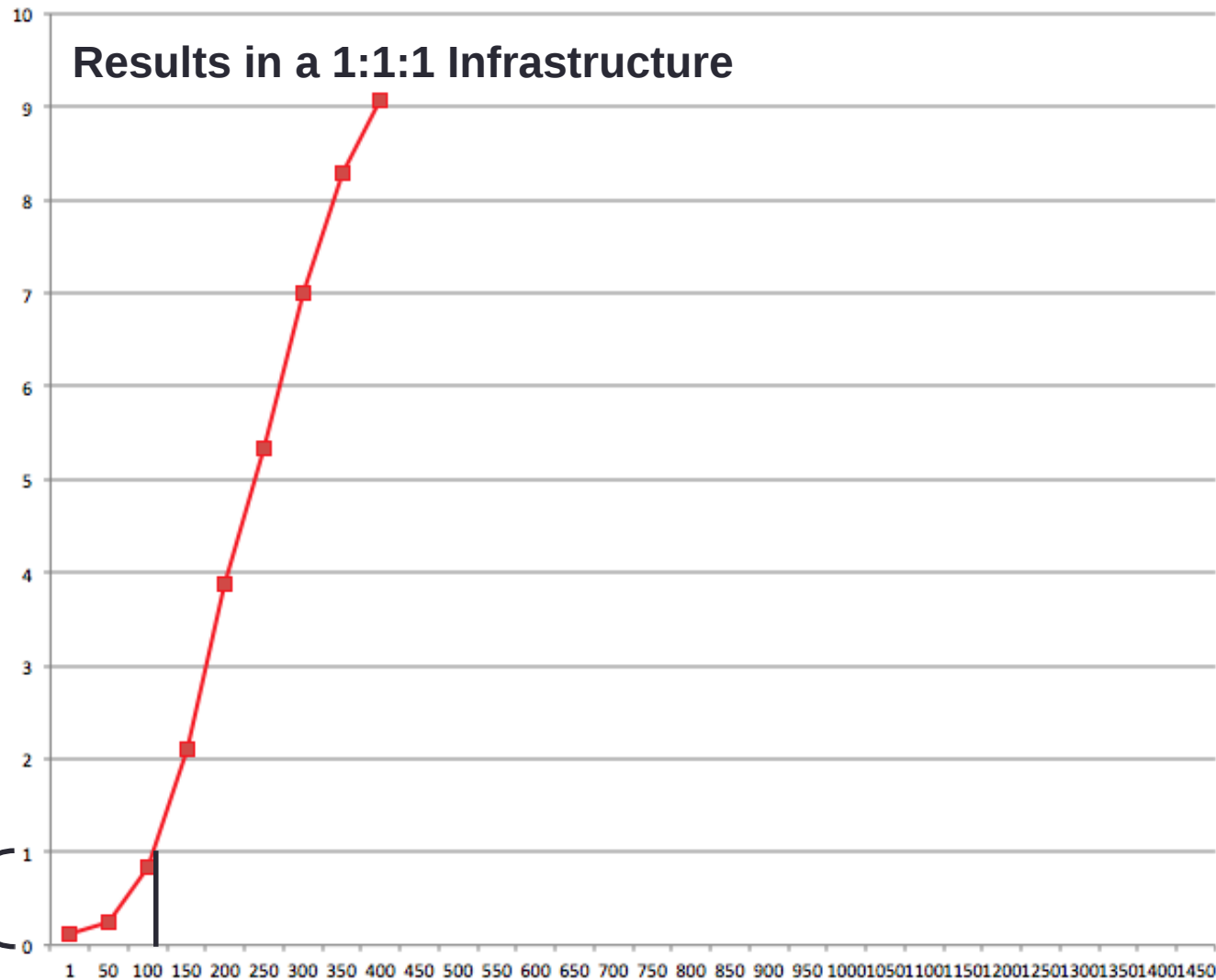
- Load a defined webpage of a lecture

- Logoff

Calculate the base load

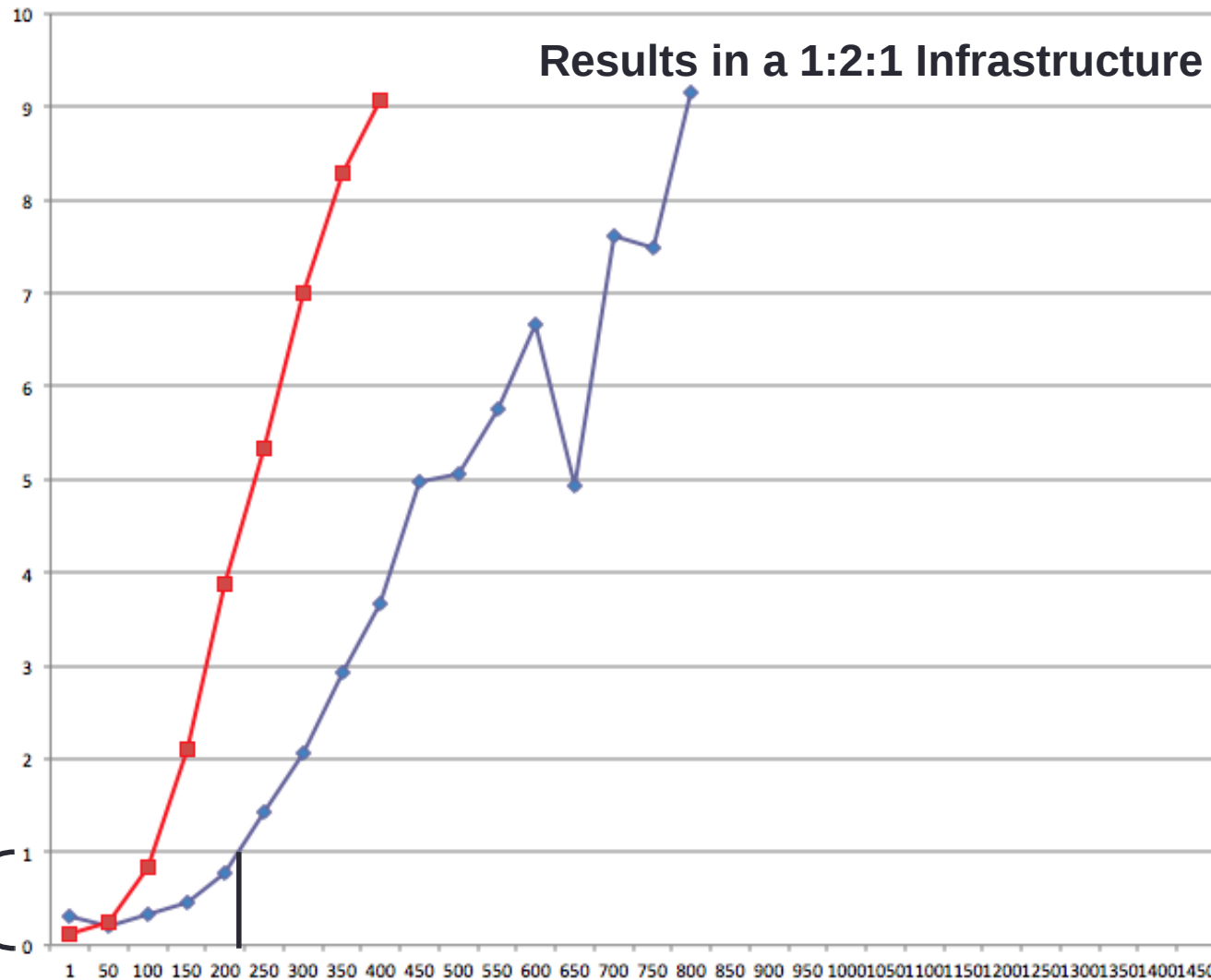
Increase app-server until “system fits”

# Performance measurement

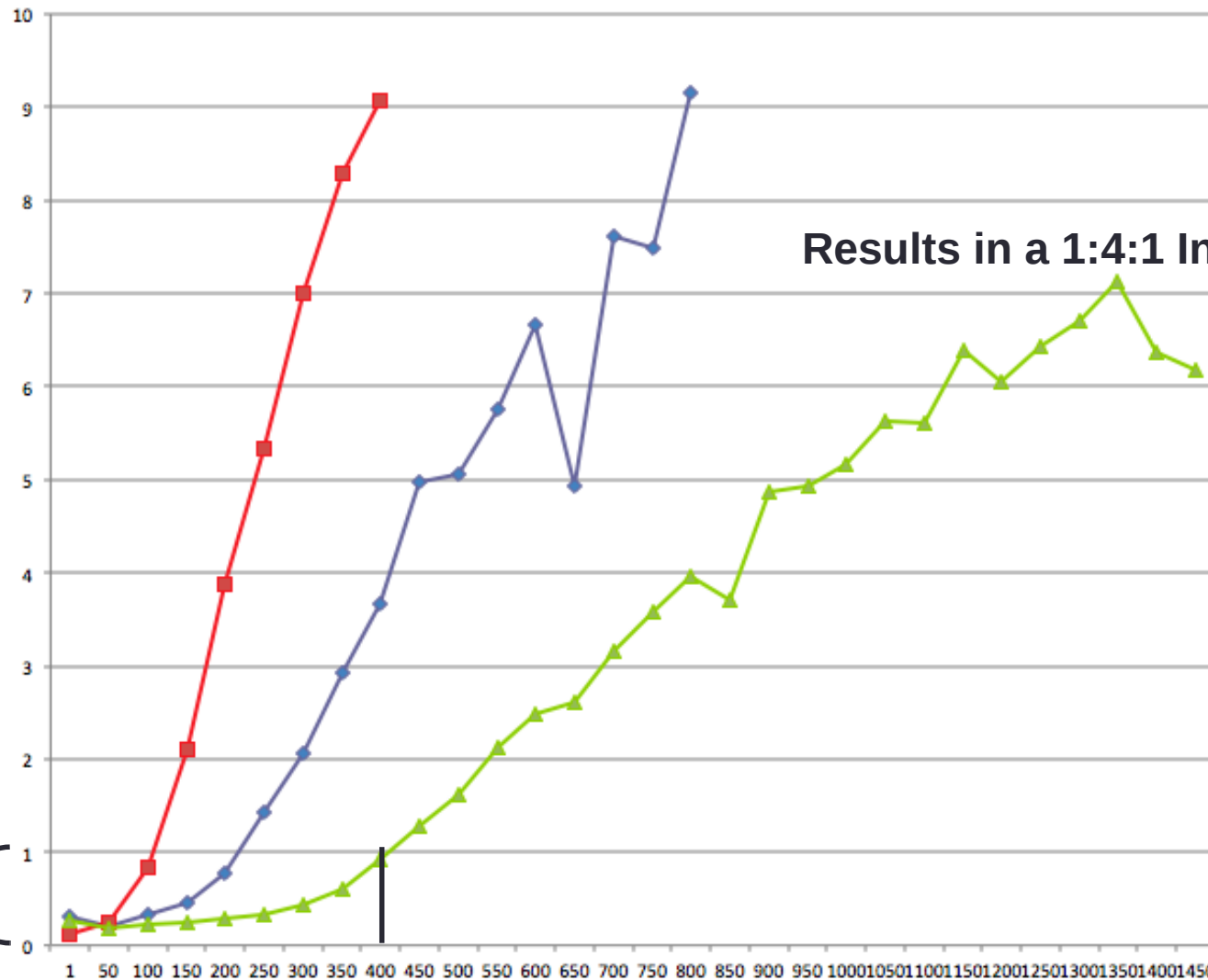




# Performance measurement



# Performance measurement



# Performance measurement

## Simulation-Result:

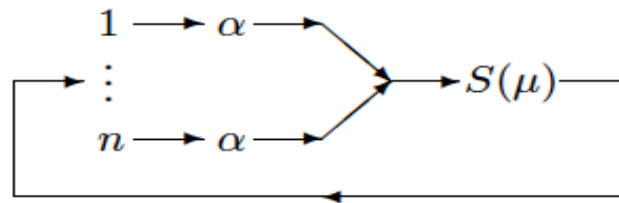
Duplication of app-server leads to duplication of maximum number of concurrent users

Average response time is cut in half and increases more slowly by duplication

# Performance modeling

Based on results and current infrastructure

Modeled system:



$n$ : # clients  
 $\alpha$ : client request rate  
 $\mu$ : service rate of server  $S$

Constraints:

service and interarrival times exponentially distributed

Our modeling process is based on classical file-server-model

Point of Interest:

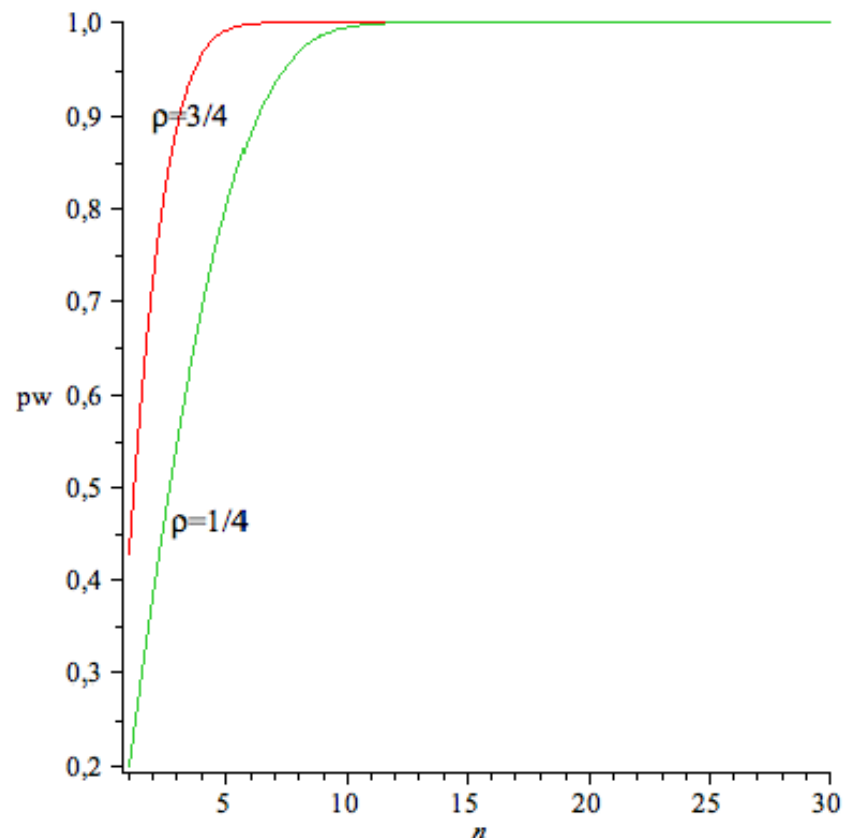
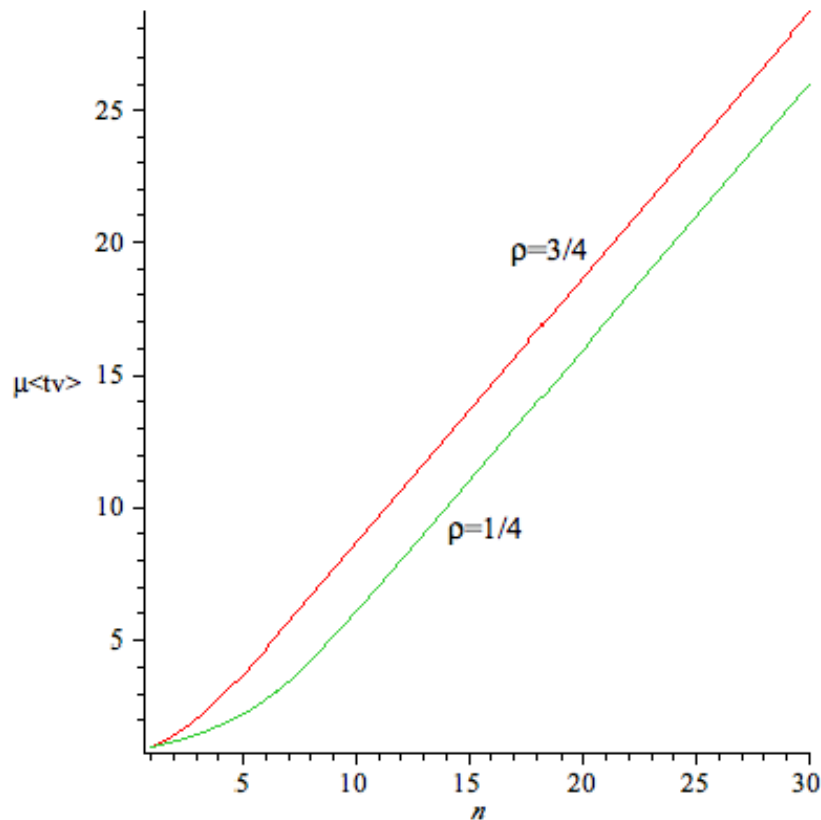
Probability of waiting  $p_w$

Average response time  $\mu\langle tv \rangle$

# Performance modeling

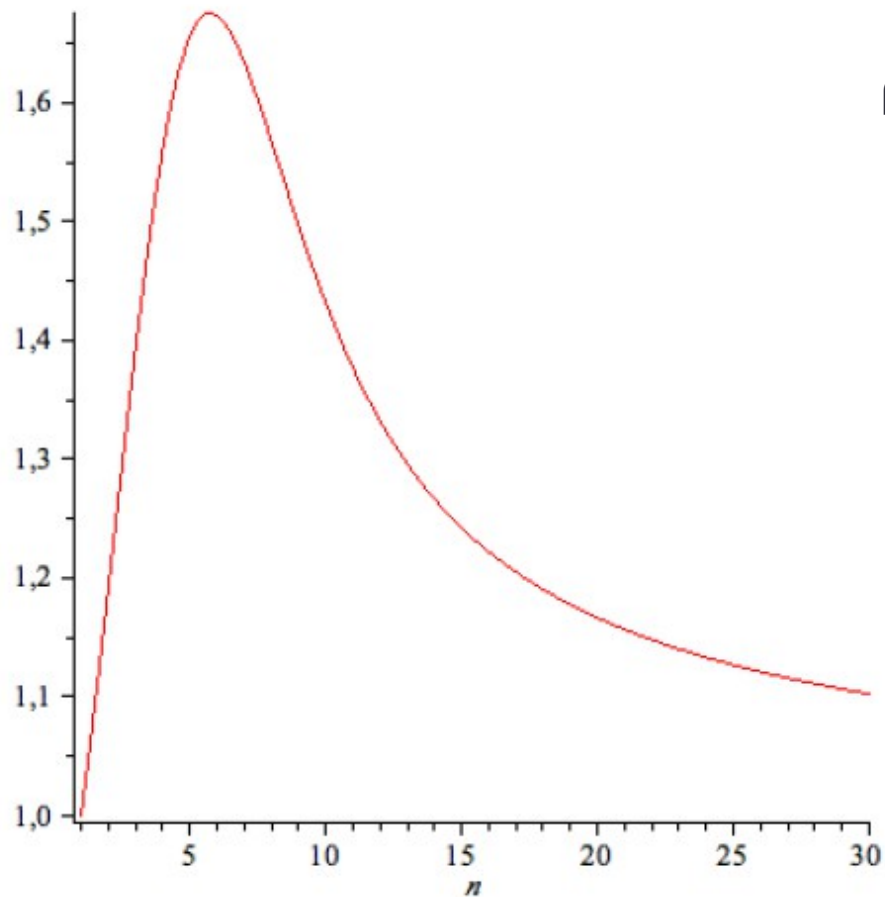
After solving equations...

$$\mu \langle t_v \rangle = \frac{n}{p_w} - \frac{1}{\rho} \quad p_w = 1 - \pi_0 = 1 - \frac{1}{S_n(\rho)} \quad \text{Load: } \rho = \alpha/\mu$$



# Performance modeling

Speedup matches observed data



$\rho=3/4$  and  $\rho=1/4$

# Performance modeling

So far only 1 server considered

Client request rate  $\alpha$  mainly triggers response time

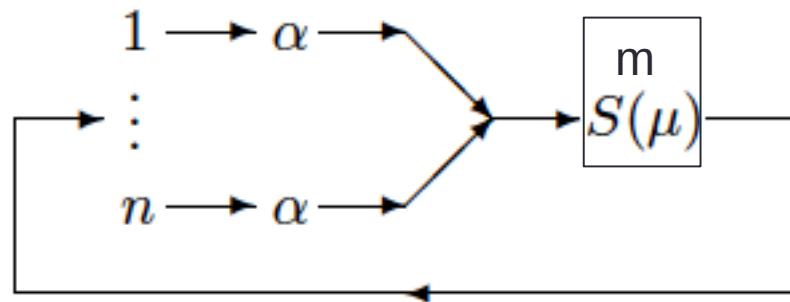
„Put“ more parallel servers into the model...

Changed server model:

Constraints:

Simplified view

no Database modeled



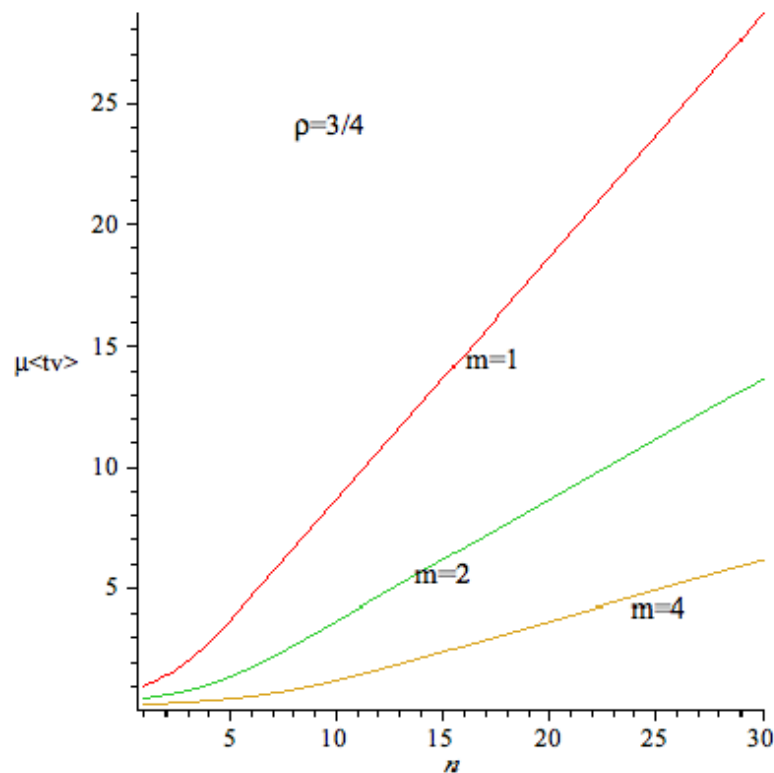
- Point of Interest:
  - Probability of waiting  $p_w(m)$
  - Average response time  $\mu\langle tv \rangle$

# Performance modeling

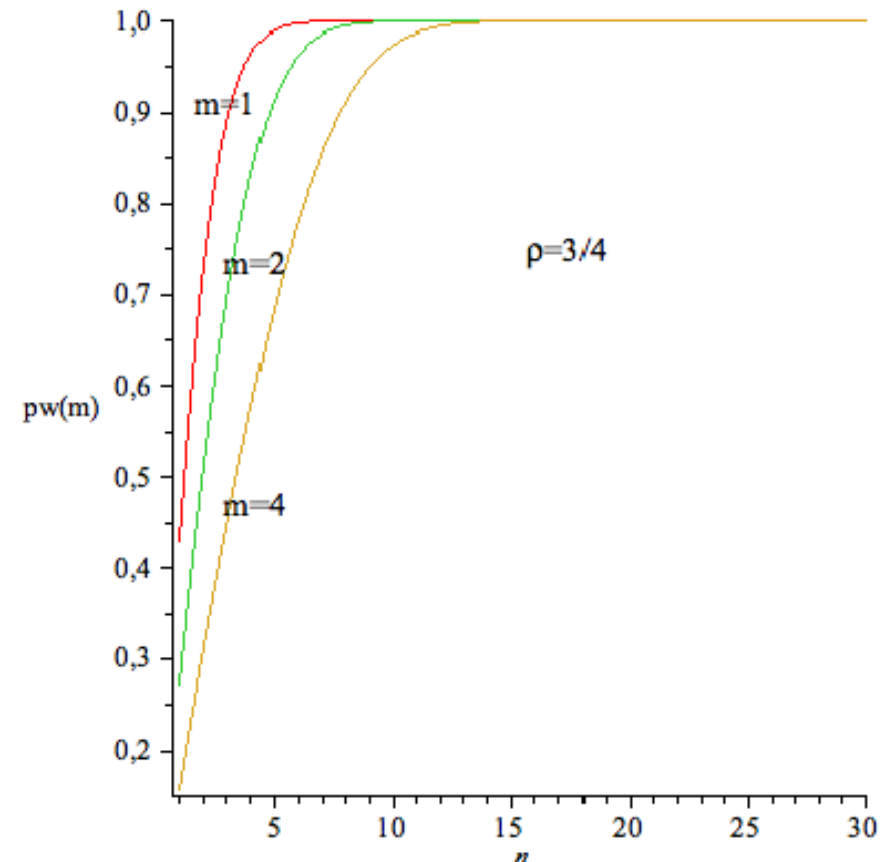
After solving equations...

$$\mu \langle t_v \rangle \mapsto \mu \langle t_v^m \rangle = \frac{(n/m)}{p_w(n, m, \rho)} - \frac{1}{\rho}$$

Load:  $\rho = \alpha/\mu = 3/4$



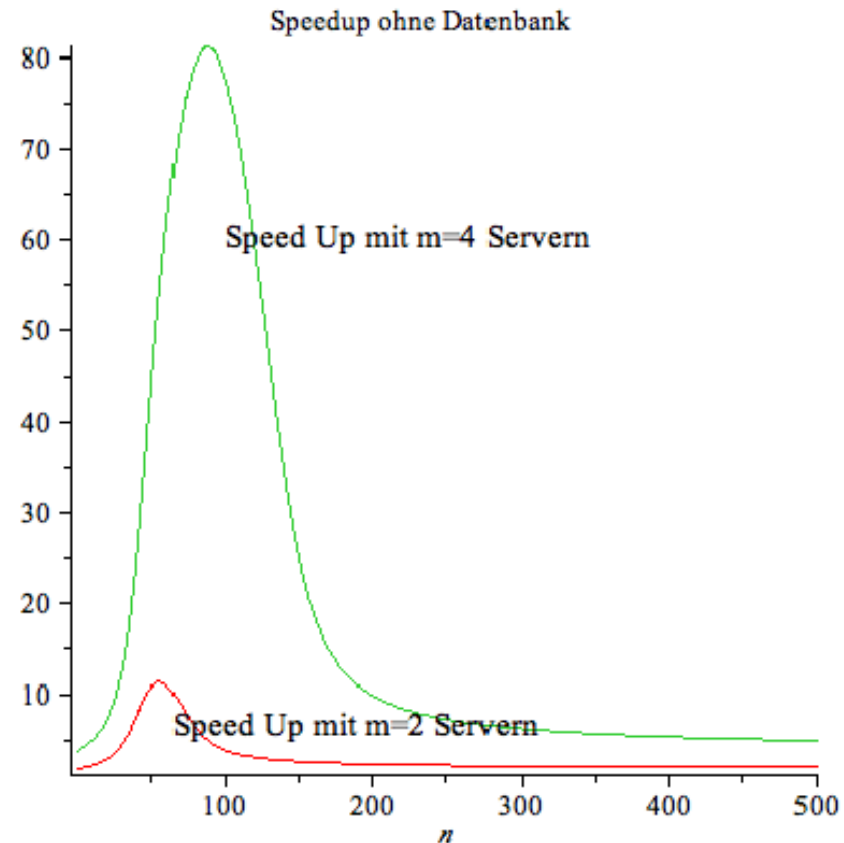
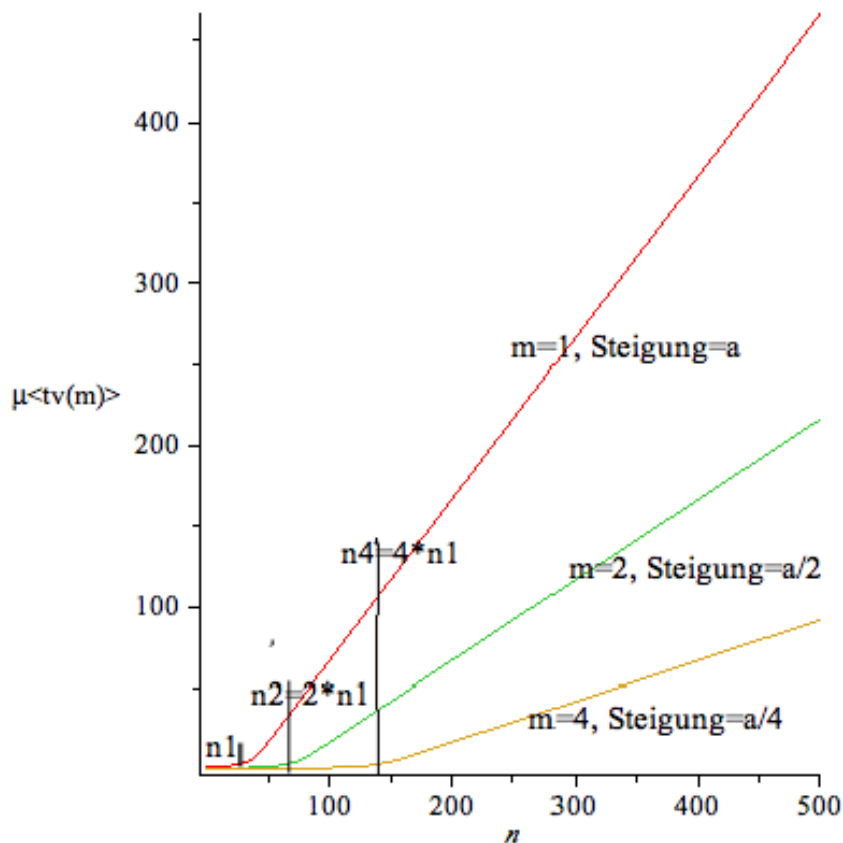
$$p_w(n, \rho) \mapsto p_w(n, m, \rho) = 1 - S_n^{-1}\left(\frac{\rho}{m}\right)$$





# Performance modeling

Speedup matches observed data  
Model adjusted ( $\alpha$  and  $\mu$ )



# Performance modeling

Qualitative aspects of model matches empirical result

Database missing in model

Extended model:

Database with own service rate

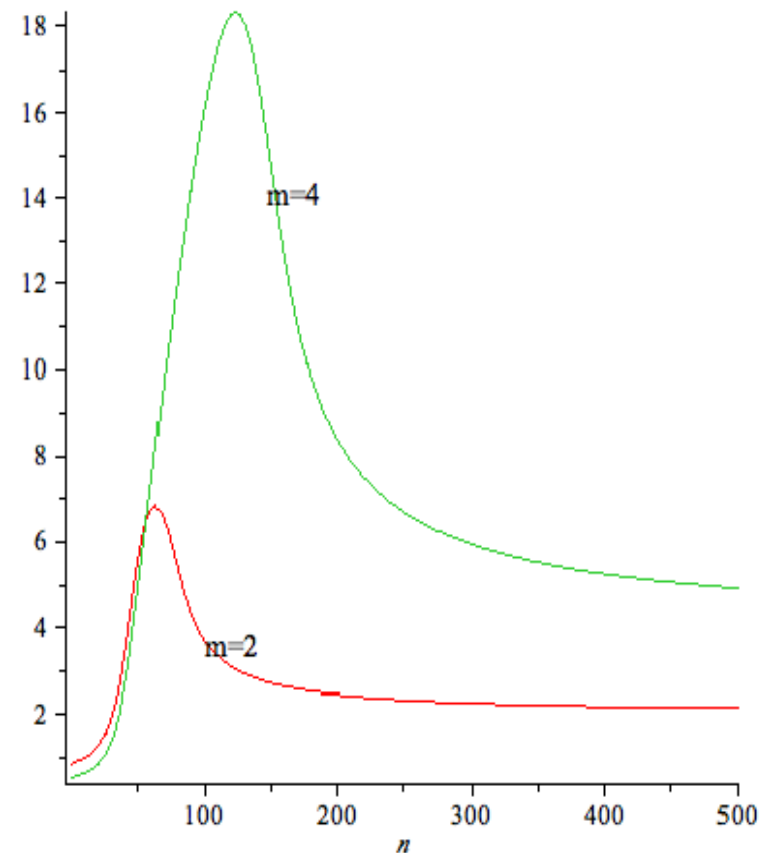
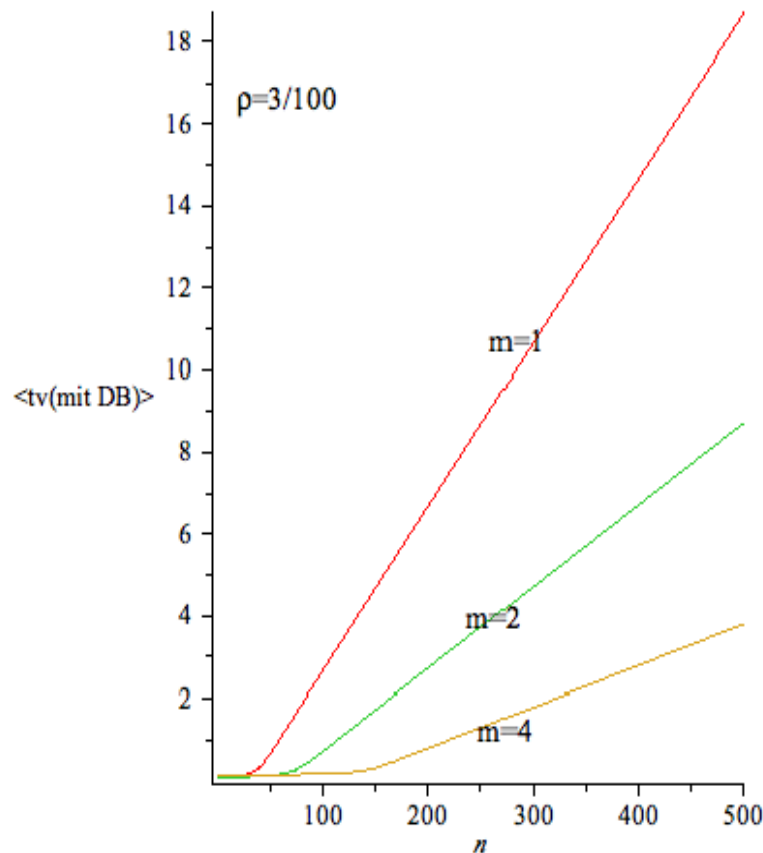
Markov models like  $M/M/1/\infty$  or  $M/G/1/\infty$  are appropriate

Load of database is fixed by observation to  $(\mu/\mu_{DB})=0.9$

Not in all requests the database is needed

# Performance modeling

- Average response time  $\mu\langle tv \rangle$  with Database and
- Corresponding Speedup
- Taking the database into account hardly changes shapes



# Summary

Performance analysis with rebuilding infrastructure  
detailed and accurate insights of a system

expensive

Performance modeling  
saves costs

Good prediction of necessary infrastructure

Reusable, but adjustment necessary

**Thank you**

**Questions?**